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Direct Coupling of Euler Flow Equations with Plate Finite Element Structures

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Introduction

IN recent years, significant advances have been made for single disciplines in both computational fluid dynamics (CFD) using finite difference approaches¹ and computational structural dynamics (CSD) using finite element methods (see Chap. 1 of Ref. 2). For aerospace vehicles, structures are dominated by internal discontinuous members such as spars, ribs, panels, and bulkheads. The finite element (FE) method, which is fundamentally based on discretization, has proven to be computationally efficient to solve aerospace structures problems. The external aerodynamics of aerospace vehicles is dominated by field discontinuities such as shock waves and flow separations. Finite difference (FD) computational methods have proven to be efficient to solve such problems.

Problems in aeroelasticity associated with nonlinear systems have been solved using both uncoupled and coupled methods.³ Uncoupled methods are less expensive but are limited to very small perturbations with moderate nonlinearity. However, aeroelastic problems of aerospace vehicles are often dominated by large structural deformations and high-flow nonlinearities. Fully coupled procedures are required to solve such aeroelastic problems accurately.

In computing aeroelasticity with coupled procedures, one needs to deal with fluid equations in an Eulerian reference system and structural equations in a Lagrangian system. Also, the structural system is physically much stiffer than the fluid system. As a result, the numerical matrices associated with structures are orders of magnitude

stiffer than those associated with fluids. Therefore, it is numerically inefficient or even impossible to solve both systems using a single system of equations. To solve this problem, Guruswamy and Yang³ presented a numerically accurate and efficient approach for two-dimensional airfoils by independently modeling fluids using FD-based transonic small perturbation (TSP) equations and structures using modal equations and coupling the solutions only at boundary interfaces between fluids and structures. This approach has been extended for more complete flow equations on the Euler/Navier-Stokes equations.⁴ The modal approach significantly reduces the number of structural unknowns to a great extent when compared to a direct use of FE equations. However, a detailed FE model is required to generate modal data particularly in the absence of experimentally measured data. One can take direct advantage of available FE data and directly couple them with flow equations. By directly using FE data, the possible errors caused by modal approximations can be avoided, and detailed results such as stresses can be computed directly.

In this work, a procedure to compute aeroelasticity by directly coupling the Euler equations for fluids and with plate finite element equations for structures is presented. The coupled equations are solved using a time-integration method. The time accuracy is maintained using moving grids that conform to aeroelastically deformed shape computed every time step. The aerodynamic forces are transferred to structures by using simple lumped load (LL) approach and also a more accurate virtual surface (VS) approach. The VS approach developed in this work can preserve the work done by aerodynamic forces due to structural deformations. The VS approach is validated by computing the aeroelastic response of a wing and comparing with experiment. All aeroelastic responses are computed at transonic Mach numbers where strong coupling between fluids and structures is required.

Fluid-Structural Interfaces

The finite element matrix form of the aeroelastic equations of motion can be written as

$$[M]\{\ddot{q}\} + [G]\{\dot{q}\} + [K]\{q\} = \{Z\} \quad (1)$$

where $[M]$, $[G]$, and $[K]$ are the global mass, damping, and stiffness matrices, respectively. $\{Z\}$ is the aerodynamic force vector corresponding to the nodal displacement vector $\{q\}$. The aerodynamic force vector $\{Z\}$ is computed by solving Euler flow equations using ENSAERO. The plate option of the ANS4 shell/plate element is used to represent the structural properties of the wing configuration.⁵

The main effort after selecting the FE model of the structure falls into computing the global force vector $\{Z\}$ of Eq. (1). $\{Z\}$ is computed by solving the Euler equations at given time t . First, the pressures are computed at all surface grid points. The forces corresponding to the nodal DOF are computed using the fluid-structural interfaces discussed in the following section.

In aeroelastic analysis, it is necessary to represent equivalent aerodynamic loads at the structural nodal points and to represent de-

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formed structural configurations at the aerodynamic grid points. In the present domain decomposition approach, coupling between the fluid and structural domains is achieved by combining the boundary data such as aerodynamic pressures and structural deflections at each time step. An analytical moving grid technique has been successfully used to deform the aerodynamic grid according to structural deflections at the end of every time step. There are several different ways to obtain the global force vector $\{Z\}$ of Eq. (1) depending on the equations used for the structural dynamic analysis.

A number of numerical procedures have been developed to exchange the necessary information between the aerodynamic and structural domains as listed in Ref. 6. Use of a bilinear interpolation and a VS interface are investigated in this study. The bilinear interpolation is same as the LL approach. In this approach, the force acting on each element of the structural mesh is first calculated, and then the element nodal force vector is obtained by distributing the total force. The global force vector is obtained by assembling the nodal force vectors of each element. In addition, the deformed configuration of the CFD grid at the surface is obtained by linearly interpolating nodal displacements at finite element nodes. This approach does not conserve the work done by the aerodynamic forces and needs fine grids for both fluids and structures to give accurate results.

An alternate to the LL approach is an improved approach based on the VS. In this approach, a mapping matrix developed by Appa⁶ is selected to accurately exchange data between the fluid and structural interface boundaries. The reason for selecting Appa's method is that the mapping matrix is general enough to accommodate changes in fluid and structural models easily. In addition, this approach conserves the work done by aerodynamic forces when obtaining the global nodal force vector. This method introduces a VS between the CFD surface grid and the finite element mesh for the wing. This VS is discretized by a number of finite elements, which are not necessarily the same elements used in the structural surface modeling.

By forcing the deformed VS to pass through the given data points of the deformed structure, a mapping matrix relating displacements at structural and aerodynamic grid points is derived as

$$[T] = \{\psi_a\} (\delta^{-1}[K] + \{\psi_s\}^T \{\psi_s\})^{-1} \{\psi_s\}^T \quad (2)$$

where $[K]$ is the free-free stiffness of the VS, ψ_s is displacement mapping from VS to structural grids, ψ_a is displacement mapping from VS to aerodynamic grids, and δ is the penalty parameter.

Then, the displacement vector at the aerodynamic grid $\{q_a\}$ can be expressed, in terms of the displacement vector at the structural nodal points q_s , as

$$\{q_a\} = [T]\{q_s\} \quad (3)$$

From the principle of virtual work, the nodal force vector $\{Z_s\}$ can be obtained as

$$\{Z_s\} = [T]^T \{Z_a\} \quad (4)$$

where $\{Z_a\}$ is the force vector at the aerodynamic grids. This procedure is illustrated in Fig. 1.

The aeroelastic equation of motion Eq. (1) is solved by a numerical integration technique based on the constant-average-acceleration method. To maintain the time accuracy, grids are regenerated every time step according to the aeroelastically deformed shape by using the moving grid capability available in Computer Code ENSAERO.

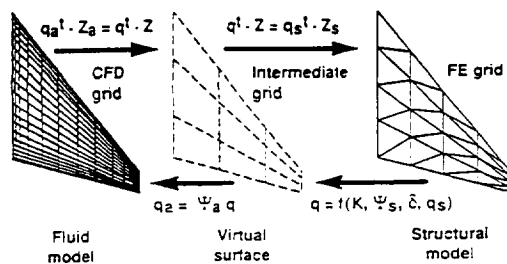


Fig. 1 Fluid-structure interfacing using virtual surface approach.

Results

To demonstrate aeroelastic computations, a typical fighter type wing is selected. For this wing transonic flutter data is available from wind-tunnel tests.⁷ In this computation, the flowfield is discretized using a C-H grid topology of size $151 \times 30 \times 35$.

This is the first time a plate FE model has been directly coupled with the Euler equations. As a result, the validity of the coupling approach will be verified by comparing the FE results with those from the previously well-validated modal analysis. In this calculation, the FE computations were made using 36 plate elements, and the modal computations were made using the first six modes of the wing. Six elements each were assigned along the chordwise and spanwise directions, respectively. Figure 2 shows the displacement responses of the leading edge at the tip obtained by both FE and modal analyses for $M_\infty = 0.854$, $p = 0.70$ psi, and $\alpha = 1.0$ deg. For this simulation, dynamic aeroelastic computations were made setting a high value for the damping coefficient so that the final results would approach steady-state conditions. The VS approach was used to calculate nodal forces for both the FE and modal analysis. Results in Fig. 2 demonstrate the validity of the coupling of plate elements with the Euler equations. The FE approach gives displacements about 0.1% higher than the modal approach. Such results are expected since the modal approach yields a structure that is stiffer than the actual one, whereas the FE approach represents the actual structural stiffness.

The accuracy of the results can depend on the type of interfaces between fluids and structures. In the following calculations, the simple LL and the more accurate VS interfaces are compared to each other, and the results are shown in Fig. 3. The wing structure was modeled using 100 ANS4 elements. An assignment of 10 elements each was made along the chordwise and spanwise directions, respectively. To discretize the VS, a four-noded, isoparametric element is used. For a given dynamic pressure of 1.0 psi and initial acceleration of 1.0×10^5 in./s, the time history of total lift on the wing is presented in Fig. 3. The total lift obtained by integrating the pressure coefficients at CFD grid points is also shown in the figure. The total lift using CFD grid points is more accurate than those from VS and

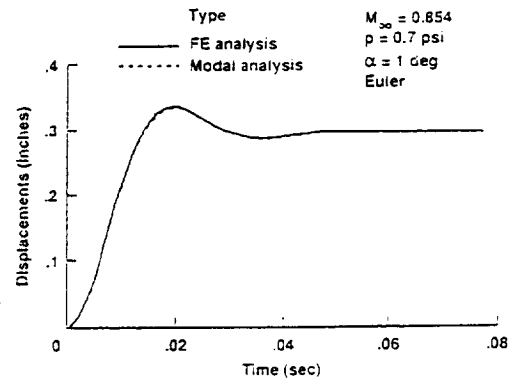


Fig. 2 Validation of finite element implementation in ENSAERO.

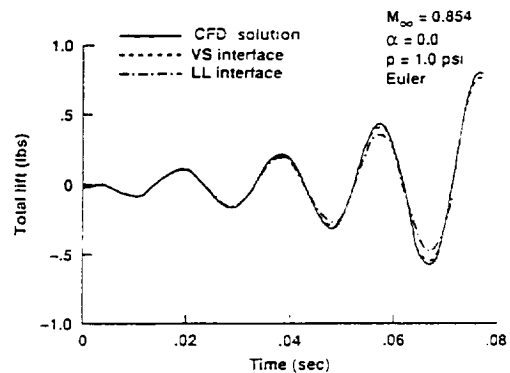


Fig. 3 Comparison of lumped load and virtual surface interfacing methods.

LL methods. Both VS and LL approaches obtain the total lift by summing the forces at the FE nodal points, which was transformed from the pressure coefficients through interfaces. The VS approach transfers pressure data more accurately than the LL approach. The LL approach shows that the response around peaks deviates from the CFD solution. For this case the LL approach shows reasonable agreement with the VS approach.

The present work has strong potential for general applications dealing with more complex geometries and complete equations. Application of this approach for wing-body configurations by using the Navier-Stokes equations is demonstrated in Ref. 8.

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